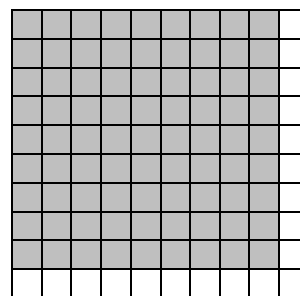


Section 1.1 Square Roots of Perfect Squares

To determine the area of a square, we multiply the side length by itself.

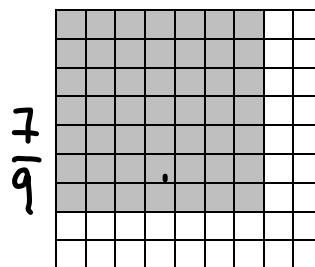
That is, we square the side length.

$$\begin{aligned}\text{Area} &= \text{side length}^2 \\ &= \left(\frac{9}{10}\right)^2 \\ &= \frac{9}{10} \times \frac{9}{10} \\ &= \frac{81}{100} \text{ units}^2\end{aligned}$$



To determine the side length of a square, we calculate the square root of its area.

$$\begin{aligned}\text{Side length} &= \sqrt{\text{Area}} \\ &= \sqrt{\frac{49}{81}} \\ &= \frac{7}{9} \text{ units}\end{aligned}$$



Squaring and taking the square root are opposite, or inverse, operations.

The side length of a square is the square root of its area.

That is, $\sqrt{\frac{225}{100}} = \frac{15 \div 5}{10 \div 5} = \frac{3}{2}$ and $\sqrt{\frac{169}{100}} = \frac{13}{10}$

We can rewrite these equations using decimals:

$$\sqrt{2.25} = 1.5 \quad \text{and} \quad \sqrt{1.69} = 1.3$$

The square roots of some fractions are repeating decimals.

Ex: $\sqrt{\frac{1}{9}} = \frac{1}{3} = 0.\overline{3} = 0.3333 \dots$

A fraction in simplest form is a perfect square if it can be written as a product of two equal fractions.

Ex: $\frac{6 \div 6}{18 \div 6} = \frac{1}{3}$ ← perf. sq.
 $\frac{1}{3}$ ← NOT perf. sq.

$\frac{6}{18}$ is not a perfect square.
 therefore

Example (1): Calculate the number whose square roots is:

a) $\frac{3}{8}$

$$\sqrt{\boxed{?}} = \frac{3}{8}$$

$$\left(\frac{3}{8}\right)^2 = \frac{3}{8} \times \frac{3}{8} = \boxed{\frac{9}{64}}$$

b) 1.8

$$\sqrt{\boxed{?}} = 1.8$$

$$(1.8)^2 = 1.8 \times 1.8 = \boxed{3.24}$$

Example (2): Is each fraction a perfect square? Explain your reasoning. *Simplest Form*

a) $\frac{8}{18} \div 2$

$$= \frac{4}{9}$$

Yes $\frac{8}{18}$ is a perf. sq.
Since, $\frac{2}{3} \times \frac{2}{3} = \frac{4}{9} = \frac{8}{18}$

b) $\frac{16}{5}$

No, $\frac{16}{5}$ is not a perf. sq. since you cannot mult. a # by itself to get $\frac{16}{5}$

c) $\frac{2}{9}$

No, $\frac{2}{9}$ is not a perf. square. Since you cannot mult. a # by itself to get $\frac{2}{9}$

Example (3): Is each decimal a perfect square? Explain your reasoning.

a) 6.25

$$\sqrt{6.25} = 2.5$$

Yes 6.25 is a perf. sq.
Since the sq. root is a TERMINATING DECIMAL

b) 0.627

$$\sqrt{0.627} = 0.79183\dots$$

0.627 is NOT a perf. square Since $\sqrt{0.627}$ is IRRATIONAL.