

6.1 Solving Equations by Using Inverse Operations – Notes

Example (1): For each statement below, write then solve an equation to determine each number.

a) Three times a number is -3.6

$$\frac{3n}{3} = \frac{-3.6}{3}$$

$$\boxed{n = -1.2}$$

b) a number divided by 4 is 1.5

$$\frac{n}{4} \times 4 = 1.5 \times 4$$

$$\boxed{n = 6}$$

Example (2): Solve, then verify each equation.

a) $4.5d - 3.2 = -18.5$

$$+3.2 \quad +3.2$$

$$\frac{4.5d}{4.5} = \frac{-15.3}{4.5}$$

$$\boxed{d = -3.4}$$

Check:
 $4.5d - 3.2 = -18.5$
 $4.5(-3.4) - 3.2 = -18.5$
 $-15.3 - 3.2 = -18.5$
 $-18.5 = -18.5 \checkmark$

b) $\frac{r}{4} + 3 = 7.2$

$$-3 \quad -3$$

$$\frac{r}{4} \times 4 = 4.2 \times 4$$

$$\boxed{r = 16.8}$$

Check:
 $\frac{16.8}{4} + 3 = 7.2$
 $4.2 + 3 = 7.2$
 $7.2 = 7.2 \checkmark$

c) $12 = -2(-1.5 - 7y)$

$$12 = 3 + 14y$$

$$\frac{9}{14} = \frac{14y}{14}$$

$$\boxed{y = \frac{9}{14}}$$

check:

$$12 \stackrel{?}{=} -2(-1.5 - 7(\frac{9}{14}))$$

$$12 \stackrel{?}{=} -2(-1.5 - 4.5)$$

$$12 \stackrel{?}{=} -2(-6)$$

$$12 = 12 \checkmark$$

d) $\frac{3}{5}(m - 2) = \frac{2}{3}$

$$\frac{3 \times 3}{5 \times 3} m - \frac{6 \times 3}{5 \times 3} = \frac{2 \times 5}{3 \times 5}$$

$$\frac{9}{15} m - \frac{18}{15} = \frac{10}{15}$$

$$9m - 18 = 10$$

$$+18 \quad +18$$

$$\frac{9m}{9} = \frac{28}{9} \quad \boxed{m = \frac{28}{9}}$$

Example (3): A rectangle has length 3.7 cm and perimeter 12.2 cm.

$$P = 2L + 2W$$

a) Write an equation that can be used to determine the width of the rectangle.

$$12.2 = 2(3.7) + 2W$$

$$12.2 = 7.4 + 2W$$

b) Solve the equation.

$$12.2 = 7.4 + 2W$$

$$\begin{array}{r} -7.4 \\ 12.2 = 7.4 + 2W \end{array}$$

$$\frac{4.8}{2} = \frac{2W}{2}$$

$$\boxed{W = 2.4}$$

c) Verify the solution.

$$12.2 \stackrel{?}{=} 7.4 + 2(2.4)$$

$$12.2 \stackrel{?}{=} 7.4 + 4.8$$

$$12.2 = 12.2$$

Example (4): Seven percent of a number is 56.7

a) Write, then solve an equation to determine the number.

$$\begin{array}{ccccccc} 7\% & \text{of} & \text{a number} & \text{is} & 56.7 \\ \downarrow & \downarrow & & \downarrow & \\ 0.07 & \times & n & = & 56.7 \end{array}$$

$$\begin{array}{r} 0.07n = 56.7 \\ \hline 0.07 \quad 0.07 \end{array}$$

$$\boxed{n = 810}$$

b) Check the solution.

$$0.07n \stackrel{?}{=} 56.7$$

$$\begin{array}{l} 0.07(810) \stackrel{?}{=} 56.7 \\ 56.7 = 56.7 \checkmark \end{array}$$